# A Reflective View on Text Similarity

Daniel Bär, Torsten Zesch, and Iryna Gurevych

Ubiquitous Knowledge Processing Lab Computer Science Department, Technische Universität Darmstadt Hochschulstrasse 10, D-64289 Darmstadt, Germany www.ukp.tu-darmstadt.de

#### Abstract

While the concept of similarity is well grounded in psychology, text similarity is less well-defined. Thus, we analyze text similarity with respect to its definition and the datasets used for evaluation. We formalize text similarity based on the geometric model of conceptual spaces along three dimensions inherent to texts: structure, style, and content. We empirically ground these dimensions in a set of annotation studies, and categorize applications according to these dimensions. Furthermore, we analyze the characteristics of the existing evaluation datasets, and use those datasets to assess the performance of common text similarity measures.

# 1 Introduction

Within the natural language processing (NLP) community, similarity between texts (*text similar-ity*, henceforth) is utilized in a wide range of tasks, e.g. automatic essay grading (Attali and Burstein, 2006) or paraphrase recognition (Tsatsaronis et al., 2010). However, *text similarity* is often used as an umbrella term covering quite different phenomena. Therefore, we formalize text similarity and analyze the datasets used for evaluation.

We argue that the seemingly simple question "How similar are two texts?" cannot be answered independently from asking *what properties make them similar*. Goodman (1972) gives a good example regarding the baggage check at an airport: While a spectator might compare bags by shape, size, or color, the pilot only focuses on a bag's weight, and the passenger compares them by destination and ownership. Similarly, texts also have certain inherent properties (*dimensions*, henceforth) that need to be considered in any attempt to judge their similarity. Consider, for example, two novels by Leo Tolstoy<sup>1</sup>. A reader may readily argue that these novels are completely dissimilar due to different plots, people, or places (i.e. dissimilar *content*). On the other hand, another reader may argue that both texts are indeed highly similar because of their *stylistic* similarities. Hence, text similarity is a loose notion unless we provide a certain frame of reference. Therefore, we introduce a formalization based on *conceptual spaces* (Gärdenfors, 2000). Furthermore, we discuss the datasets used for evaluating text similarity measures. We analyze the properties of each dataset by means of annotation studies and a critical view on the performance of common similarity measures.

## 2 Formalization

In psychology, similarity is well formalized and captured in formal models such as the settheoretic model (Tversky, 1977) or the geometric model (Widdows, 2004). In an attempt to overcome the traditionally loose definition of text similarity, we rely on a conceptual framework based on conceptual spaces (Gärdenfors, 2000). In this model, objects are represented in a number of geometric spaces. For example, potential spaces related to countries are *political affinity* and *geo*graphical proximity. In order to adapt this model to texts, we need to define explicit spaces (i.e. dimensions) suitable for texts. Therefore, we analyzed common NLP tasks with respect to the relevant dimensions of similarity, and then conducted annotation studies to ground them empirically.

Table 1 gives an overview of common NLP tasks and their relevant dimensions: *structure*, *style*, and *content*. *Structure* thereby refers to the internal developments of a given text, e.g. the order of sections. *Style* refers to grammar, usage, mechanics, and lexical complexity (Attali and Burstein, 2006). *Content* addresses all facts and

<sup>&</sup>lt;sup>1</sup>A famous 19th century Russian writer of realist fiction and philosophical essays

Task	str	sty	с
Authorship Classification		$\checkmark$	
Automatic Essay Scoring	$\checkmark$	$\checkmark$	$\checkmark$
Information Retrieval	$\checkmark$	$\checkmark$	$\checkmark$
Paraphrase Recognition			$\checkmark$
Plagiarism Detection		$\checkmark$	$\checkmark$
Question Answering			$\checkmark$
Short Answer Grading	$\checkmark$	$\checkmark$	$\checkmark$
Summarization	$\checkmark$		$\checkmark$
Text Categorization			$\checkmark$
Text Segmentation	$\checkmark$		$\checkmark$
Text Simplification	$\checkmark$		$\checkmark$
Word Sense Alignment			$\checkmark$

Table 1: Classification of common NLP tasks with respect to the relevant dimensions of text similarity: *structure (str)*, *style (sty)*, and *content (c)* 

their relationships within a text. For example, the task of automatic essay scoring (Attali and Burstein, 2006) typically not only requires the essay to be about a certain topic (*content* dimension), but also an adequate style and a coherent structure are necessary. However, in authorship classification (Holmes, 1998) only *style* is important.

Taking this dimension-centric view on text similarity also opens up new perspectives. For example, standard information retrieval usually considers only the *content* dimension (keyword overlap between query and document). However, a scholar in digital humanities might be interested in texts that are similar to a reference document with respect to style and structure, while texts with similar content are of minor interest. In this paper, we only address dimensions inherent to texts, and do not consider dimensions such as user intentions.

#### 2.1 Empirical Grounding

In order to empirically ground the proposed dimensions of text similarity, we conducted a number of exemplary annotation studies. The results show that annotators indeed distinguish between different dimensions of text similarity.

**Content vs. Structure** In this study, we used the dataset by Lee et al. (2005) that contains pairwise human similarity judgments for 1,225 text pairs. We selected a subset of 50 pairs with a uniform distribution of judgments across the whole similarity range. We then asked three annotators: "How similar are the given texts?" We then computed the Spearman correlation of each annotator's ratings with the gold standard:  $\rho_{A_1} = 0.83$ ,  $\rho_{A_2} = 0.65$ , and  $\rho_{A_3} = 0.85$ . The much lower correlation of

the annotator  $A_2$  indicates that a different dimension might have been used to judge similarity.

To further investigate this issue, we asked the annotators about the reasons for their judgments.  $A_1$  and  $A_3$  consistently focused only on the content of the texts and completely disregarded other dimensions.  $A_2$ , however, was also taking structural similarities into account, e.g. two texts were rated highly similar because of the way they are organized: First, an introduction to the topic is given, then a quotation is stated, then the text concludes with a certain reaction of the acting subject.

**Content vs. Style** The annotators in the previous study only identified the dimensions content and structure. Style was not addressed, as the text pairs were all of similar style, and hence that dimension was not perceived as salient. Thus, we selected 10 pairs of short texts from Wikipedia (WP) and Simple Wikipedia<sup>2</sup> (SWP). We used the first paragraphs of WP articles and the full texts of SWP articles to obtain pairs of similar length. Pairs were formed in all combinations (WP-WP, SWP-WP, and SWP-SWP) to ensure that both similarity dimensions were salient for some pairs. For example, an article from SWP and one from WP about the same topic share the same content, but are different in style, while two articles from SWP have a similar style, but different content.

We then asked three annotators to rate each pair according to the *content* and *style* dimensions. The results show that WP-WP and SWP-SWP pairs are perceived as stylistically similar, while WP-SWP pairs are seen similar with respect to their content.

#### 2.2 Discussion

The results demonstrate that humans indeed distinguish the major dimensions of text similarity. Also, they seem intuitively able to find an appropriate dimension of comparison for a given text collection. Smith and Heise (1992) refer to that as *perceived similarity* which "changes with changes in selective attention to specific perceptual properties." Selective attention can be modeled using dimension-specific similarity measures. The scores for all dimensions are computed in parallel, and then summed up for each text pair.<sup>3</sup> Thereby, we automatically obtain the discriminating dimension (see Figure 1). A, B, and C are documents of

<sup>&</sup>lt;sup>2</sup>Articles written in Simple English use a limited vocabulary and easier grammar than the standard Wikipedia.

<sup>&</sup>lt;sup>3</sup>The last step requires all measures to be normalized.

Dataset	Text Type / Domain	Length in Terms (Ø)	# Pairs	Rating Scale	# Judges per Pair
<b>30 Sentence Pairs</b> (Li et al., 2006) <b>50 Short Texts</b> (Lee et al., 2005)	Concept Definitions News (Politics)	5–33 (11) 45–126 (80)	30 1,225	0–4 1–5	32 8–12
<b>Computer Science Assignments</b> (Mohler and Mihalcea, 2009)	Computer Science	1–173 (18)	630	0–5	2
<b>Microsoft Paraphrase Corpus</b> (Dolan et al., 2004)	News	5–31 (19)	5,801	binary	2–3

Table 2: Statistics for text similarity evaluation datasets



Figure 1: Combination of specialized text similarity measures to determine the salient dimension. Left: Adding document D makes *content* salient. Right: Adding document E makes *style* salient.

the same style but rather different content (as indicated by the comparable height of the stacked bars). Adding another text D of the very same style, but where the content is rather similar to B, changes the situation to what is shown in Figure 1 (left). The pair BD stands out as its aggregated score is significantly higher than that of the others. In contrast, adding document E which is written with a different style, results in the situation as shown in Figure 1 (right). Even though B and E have rather similar content, the content dimension will not become salient because of the dominance of the style dimension. Consequently, the better measures for a certain dimension are available, the better this automatic discrimination will work. Developing such dimension-specific measures, however, requires evaluation datasets which are explicitly annotated according to those dimensions. In the next section, we analyze whether the existing datasets already fulfill this requirement.

#### **3** Evaluation Datasets

Four datasets are commonly used for evaluation (see Table 2). They contain text pairs together with human judgments about their perceived similarity. However, none of those datasets has yet undergone a thorough analysis with respect to the dimensions of text similarity encoded therein.

# 3.1 30 Sentence Pairs

Li et al. (2006) introduced 65 sentence pairs which are based on the noun pairs by Rubenstein and Goodenough (1965). Each noun was replaced by its definition from Collins Cobuild English Dictionary (Sinclair, 2001). The dataset contains judgments from 32 subjects on *how similar in meaning* one sentence is to another. Li et al. (2006) selected 30 pairs to reduce the bias in the frequency distribution (*30 Sentence Pairs*, henceforth).

We conducted a re-rating study to evaluate whether text similarity judgments are stable across time and subjects. We collected 10 judgments per pair asking: "How close do these sentences come to meaning the same thing?"<sup>4</sup> The Spearman correlation of the aggregated results with the original scores is  $\rho = 0.91$ . We conclude that text similarity judgments are stable across time and subjects. It also indicates that humans indeed share a common understanding on what makes texts *similar*.

In order to better understand the characteristics of this dataset, we performed another study. For each text pair we asked the annotators: "Why did people agree that these two sentences are (not) close in meaning?" We collected 10 judgments per pair in the same crowdsourcing setting as before.

To our surprise, the annotators only used lexical semantic relations between *terms* to justify the similarity relation between *texts*. For example, the text pairs about tool/implement and cemetery/graveyard were consistently said to be *synonymous*. We conclude that – in this setting – humans reduce *text* similarity to *term* similarity.

As the text pairs are originally based on term pairs, we computed the Spearman correlation between the text pair scores and the original term pair scores. The very high correlation of  $\rho = 0.94$ shows that annotators indeed judged the similarity between *terms* rather than *texts*. We conclude

<sup>&</sup>lt;sup>4</sup>Same question as in the original study by Li et al. (2006). We used Amazon Mechanical Turk via CrowdFlower.

Measure	r	ρ
Cosine Baseline	.81	.83
Term Pair Heuristic	.83	.84
ESA (Wikipedia)	.61	.77
ESA (Wiktionary)	.77	.82
ESA (WordNet)	.75	.80
Kennedy and Szpakowicz (2008) LSA (Tsatsaronis et al., 2010) OMIOTIS (Tsatsaronis et al., 2010) STASIS (Li et al., 2006) STS (Islam and Inkpen, 2008)	.87 .84 .86 .82 .85	.87 .89 .81 .84

Table 3: Results on the 30 Sentence Pairs dataset

that this dataset encodes the content dimension of similarity, but a rather constrained one.

**Evaluation Results** Table 3 shows the results of state of the art similarity measures obtained on this dataset. We used a cosine baseline and implemented an additional baseline which disregards the actual texts and only takes the target noun of each sentence into account. We computed their pairwise term similarity using the metric by Lin (1998) on WordNet (Fellbaum, 1998). Our heuristic achieves Pearson r = 0.83 and Spearman  $\rho = 0.84$ . The block of results in the middle shows our implementation of Explicit Semantic Analysis (ESA) (Gabrilovich and Markovitch, 2007) using different knowledge sources (Zesch et al., 2008). The bottom rows show scores previously obtained and reported in the literature. None of the measures significantly<sup>5</sup> outperforms the baselines. Given the limitation of encoding rather term than text similarity and the fact that the dataset is also very small (30 pairs), it is questionable whether it is a suitable evaluation dataset for *text* similarity.

#### 3.2 50 Short Texts

The dataset by Lee et al. (2005) comprises 50 relatively short texts (45 to 126 words<sup>6</sup>) which contain newswire from the political domain. In analogy to the study in Section 3.1, we performed an annotation study to show whether the encoded judgments are stable across time and subjects. We asked three annotators to rate *"How similar are the given texts?"*. We used the same uniformly distributed subset as in Section 2.1. The resulting Spearman correlation between the aggregated results of the annotators and the original scores is

Measure	r
Cosine Baseline	.56
ESA (Wikipedia)	.46
ESA (Wiktionary)	.53
ESA (WordNet)	.59
ESA (Gabrilovich and Markovitch, 2007)	.72
LSA (Lee et al., 2005)	.60
WikiWalk (Yeh et al., 2009)	.77

Table 4: Results on the 50 Short Texts dataset. Statistically significant<sup>7</sup> improvements in bold.

 $\rho = 0.88$ . This shows that judgments are quite stable across time and subjects.

In Section 2.1, two annotators had a contentcentric view on similarity while one subject also considered structural similarity important. When combining only the two content-centric annotators, the correlation is  $\rho = 0.90$ , while it is much lower for the other annotator. Thus, we conclude that this dataset encodes the content dimension of text similarity.

**Evaluation Results** Table 4 summarizes the results obtained on this dataset. We used a cosine baseline, and our implementation of ESA applied to different knowledge sources. The results at the bottom are scores previously obtained and reported in the literature. All of them significantly outperform the baseline.<sup>7</sup> In contrast to the *30 Sentence Pairs*, this dataset encodes a broader view on the content dimension of similarity. It obviously contains text pairs that are similar (or dissimilar) for reasons beyond partial string overlap. Thus, the dataset might be used to intrinsically evaluate text similarity measures.

However, the distribution of similarity scores in this dataset is heavily skewed towards low scores, with 82% of all term pairs having a text similarity score between 1 and 2 on a 1–5 scale. This limits the kind of conclusions that can be drawn as the number of the pairs in the most interesting class of highly similar pairs is actually very small.

Another observation is that we were not able to reproduce the ESA score on Wikipedia reported by Gabrilovich and Markovitch (2007). We found that the difference probably relates to the cut-off value used to prune the vectors as reported by Yeh et al. (2009). By tuning the cut-off value, we could improve the score to 0.70, which comes very close to the reported score of 0.72. However, as this tun-

 $<sup>{}^{5}\</sup>alpha = .05$ , Fisher Z-value transformation

<sup>&</sup>lt;sup>6</sup>Lee et al. (2005) report the shortest document having 51 words probably due to a different tokenization strategy.

 $<sup>^{7}\</sup>alpha = .01$ , Fisher Z-value transformation

Measure	r
Cosine Baseline	.44
ESA (Mohler and Mihalcea, 2009)	.47
LSA (Mohler and Mihalcea, 2009)	.43
Mohler and Mihalcea (2009)	.45

 Table 5: Results on the Computer Science Assignments dataset

ing is done directly on the evaluation dataset, it probably overfits the cut-off value to the dataset.

## 3.3 Computer Science Assignments

The dataset by Mohler and Mihalcea (2009) was introduced for assessing the quality of short answer grading systems in the context of computer science assignments. The dataset comprises 21 questions, 21 reference answers and 630 student answers. The answers were graded by two teachers – not according to stylistic properties, but to the extent the content of the student answers matched with the content of the reference answers.

**Evaluation Results** We summarize the results obtained on this dataset in Table 5. The scores are reported without relevance feedback (Mohler and Mihalcea, 2009) which distorts results by changing the reference answers. None of the measures significantly<sup>8</sup> outperforms the baseline. This is not overly surprising, as the textual similarity between the reference and the student answer only constitutes part of what makes an answer the correct one. More sophisticated measures that also take lexical semantic relationships between terms into account might even worsen the results, as typically a specific answer is required, not a similar one. We conclude that similarity measures can be used to grade assignments, but it seems questionable whether this dataset is suited to draw any conclusions on the performance of similarity measures outside of this particular task.

#### 3.4 Microsoft Paraphrase Corpus

Dolan et al. (2004) introduced a dataset of 5,801 sentence pairs taken from news sources on the Web. They collected binary judgments from 2–3 subjects whether each pair captures a paraphrase relationship or not (83% interrater agreement). The dataset has been used for evaluating text similarity measures as, by definition, paraphrases need to be similar with respect to their content.

Measure	F-measure
Cosine Baseline	.81
Majority Baseline	.80
ESA (Wikipedia)	.80
LSA (Mihalcea et al., 2006)	.81
Mihalcea et al. (2006)	.81
OMIOTIS (Tsatsaronis et al., 2010)	.81
PMI-IR (Mihalcea et al., 2006)	.81
Ramage et al. (2009)	.80
STS (Islam and Inkpen, 2008)	.81
Finch et al. (2005)	.83
Qiu et al. (2006)	.82
Wan et al. (2006)	.83
Zhang and Patrick (2005)	.81

Table 6: Results on Microsoft Paraphrase Corpus

**Evaluation Results** We summarize the results obtained on this dataset in Table 6. As detecting paraphrases is a classification task, we use an additional majority baseline which classifies all results according to the predominant class of true paraphrases. The block of results in the middle contains measures that are not specifically tailored towards paraphrase recognition. None of them beats the cosine baseline. The results at the bottom show measures which are specifically tailored towards the detection of a bidirectional entailment relationship. None of them, however, significantly outperforms the cosine baseline. Obviously, recognizing paraphrases is a very hard task that cannot simply be tackled by computing text similarity, as sharing similar content is a necessary, but not a sufficient condition for detecting paraphrases.

## 3.5 Discussion

We showed that all four datasets encode the content dimension of text similarity. The Computer Science Assignments dataset and the Microsoft Paraphrase Corpus are tailored quite specifically to a certain task. Thereby, factors exceeding the similarity of texts are important. Consequently, none of the similarity measures significantly outperformed the cosine baseline. The evaluation of similarity measures on these datasets is hence questionable outside of the specific application scenario. The 30 Sentence Pairs dataset was found to rather represent the similarity between terms than texts. Obviously, it is not suited for evaluating text similarity measures. However, the 50 Short Texts dataset currently seems to be the best choice. As it is heavily skewed towards low similarity scores, though, the conclusions that can be drawn from the results are limited. Further datasets are

 $<sup>^{8}\</sup>alpha = .05$ , Fisher Z-value transformation

necessary to guide the development of measures along other dimensions such as *structure* or *style*.

#### 4 Conclusions

In this paper, we reflected on *text similarity* as a foundational technique for a wide range of tasks. We argued that while *similarity* is well grounded in psychology, *text similarity* is less well-defined. We introduced a formalization based on *conceptual spaces* for modeling text similarity along explicit dimensions inherent to texts. We empirically grounded these dimensions by annotation studies and demonstrated that humans indeed judge similarity along different dimensions. Furthermore, we discussed common evaluation datasets and showed that it is of crucial importance for text similarity measures to address the correct dimensions. Otherwise, these measures fail to outperform even simple baselines.

We propose that future studies aiming at collecting human judgments on text similarity should *explicitly* state which dimension is targeted in order to create reliable annotation data. Further evaluation datasets annotated according to the *structure* and *style* dimensions of text similarity are necessary to guide further research in this field.

#### Acknowledgments

This work has been supported by the Volkswagen Foundation as part of the Lichtenberg-Professorship Program under grant No. I/82806, and by the Klaus Tschira Foundation under project No. 00.133.2008. We thank György Szarvas for sharing his insights into the ESA similarity measure with us.

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